Unstructured Meshing Technologies

Presented to ATPESC 2020 Participants

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ATPESC Numerical Software Track







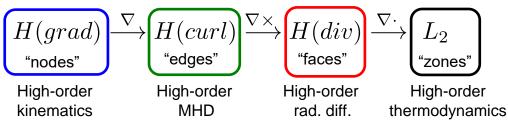


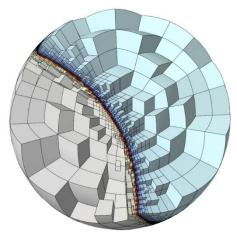




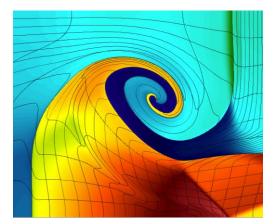
Finite elements are a good foundation for large-scale simulations on current and future architectures

- Backed by well-developed theory.
- Naturally support unstructured and curvilinear grids.
- High-order finite elements on high-order meshes
 - Increased accuracy for smooth problems
 - Sub-element modeling for problems with shocks
 - Bridge unstructured/structured grids
 - Bridge sparse/dense linear algebra
 - FLOPs/bytes increase with the order
- Demonstrated match for compressible shock hydrodynamics (BLAST).
- Applicable to variety of physics (DeRham complex).





Non-conforming mesh refinement on high-order curved meshes

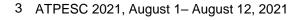


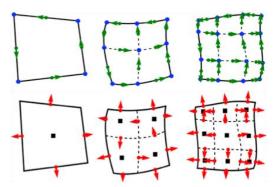
8th order Lagrangian hydro simulation of a shock triple-point interaction

Modular Finite Element Methods (MFEM)

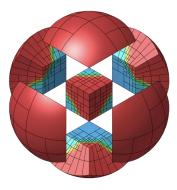
MFEM is an open-source C++ library for scalable FE research and fast application prototyping

- Triangular, quadrilateral, tetrahedral and hexahedral; volume and surface meshes
- Arbitrary order curvilinear mesh elements
- Arbitrary-order H1, H(curl), H(div)- and L2 elements
- Local conforming and non-conforming refinement
- NURBS geometries and discretizations
- Bilinear/linear forms for variety of methods (Galerkin, DG, DPG, Isogeometric, ...)
- Integrated with: HYPRE, SUNDIALS, PETSc, SUPERLU, PUMI, Vislt, Spack, xSDK, OpenHPC, and more ...
- Parallel and highly performant
- Main component of ECP's co-design Center for Efficient Exascale Discretizations (CEED)
- Native "in-situ" visualization: GLVis, glvis.org





Linear, quadratic and cubic finite element spaces on curved meshes



mfem.org (v3.4, May/2018)



Mesh

```
// 2. Read the mesh from the given mesh file. We can handle triangular,
64
       11
              quadrilateral, tetrahedral, hexahedral, surface and volume meshes with
65
       11
              the same code.
66
       Mesh *mesh;
67
       ifstream imesh(mesh file);
       if (!imesh)
68
69
70
71
72
73
74
75
76
77
78
79
80
81
82
83
84
       -{
          cerr << "\nCan not open mesh file: " << mesh file << '\n' << endl;
          return 2:
       mesh = new Mesh(imesh, 1, 1);
       imesh.close();
       int dim = mesh->Dimension();
       // 3. Refine the mesh to increase the resolution. In this example we do
       11
              'ref levels' of uniform refinement. We choose 'ref levels' to be the
       11
              largest number that gives a final mesh with no more than 50,000
       11
              elements.
           int ref levels =
              (int)floor(log(50000./mesh->GetNE())/log(2.)/dim);
           for (int 1 = 0; 1 < ref_levels; 1++)</pre>
85
              mesh->UniformRefinement();
86
```

Finite element space

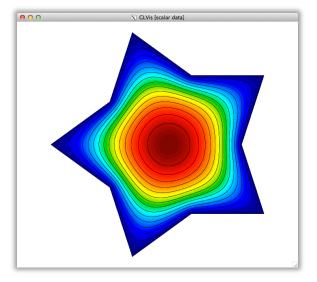


Linear solve

130	#ifndef MFEM USE SUITESPARSE
131	// 8. Define a simple symmetric Gauss-Seidel preconditioner and use it to
132 133	// solve the system Ax=b with PCG.
133	GSSmoother M(A);
134	PCG(A, M, *b, x, 1, 200, 1e-12, 0.0);
135	#else
136	// 8. If MFEM was compiled with SuiteSparse, use UMFPACK to solve the system.
137	UMFPackSolver umf solver;
138	umf solver.Control[UMFPACK ORDERING] = UMFPACK ORDERING METIS;
139	umf solver.SetOperator(A);
140	umf solver.Mult(*b, x);
141	#endif

Visualization

// 10. Send the solution by socket to a GLVis server. 152 153 if (visualization) 154 char vishost[] = "localhost"; 155 int visport = 19916; 156 157 socketstream sol_sock(vishost, visport); 158 sol_sock.precision(8); 159 sol sock << "solution\n" << *mesh << x << flush; 160



- works for any mesh & any H1 order
- builds without external dependencies

4 ATPESC 2021, August 1– August 12, 2021

Mesh

```
63
      // 2. Read the mesh from the given mesh file. We can handle triangular,
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         return 2;
72
       }
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79
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             elements.
81
       Ł
82
          int ref levels =
83
             (int)floor(log(50000./mesh->GetNE())/log(2.)/dim);
84
          for (int 1 = 0; 1 < ref levels; 1++)
85
             mesh->UniformRefinement();
86
       Ł
```

Finite element space

88 89	
90	<pre>// instead use an isoparametric/isogeometric space.</pre>
91	
92	if (order > 0)
93	<pre>fec = new H1 FECollection(order, dim);</pre>
94	<pre>else if (mesh->GetNodes())</pre>
95	<pre>fec = mesh->GetNodes()->OwnFEC();</pre>
96	else
97	<pre>fec = new H1 FECollection(order = 1, dim);</pre>
98	
99	

Initial guess, linear/bilinear forms

10 10 10	2 // the FEM linear system, which in this case is (1,phi_i) where phi_i are 3 // the basis functions in the finite element fespace.
104 105 106	5 ConstantCoefficient one(1.0);
10	<pre>7 b->Assemble();</pre>
100 100 110	9 // 6. Define the solution vector x as a finite element grid function // corresponding to fespace. Initialize x with initial guess of zero,
112	
114 119 110 110 110 110 110 110	// 7. Set up the bilinear form a(.,.) on the finite element space // corresponding to the Laplacian operator -Delta, by adding the Diffusion domain integrator and imposing homogeneous Dirichlet boundary // conditions. The boundary conditions are implemented by marking all the boundary attributes from the mesh as essential (Dirichlet). After assembly and finalizing we extract the corresponding sparse matrix A.
12: 12: 12:	2 a->AddDomainIntegrator(new DiffusionIntegrator(one));
124	<pre>4 Array<int> ess_bdr(mesh->bdr_attributes.Max());</int></pre>
12	

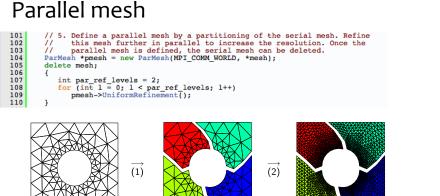
Linear solve

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135	
136	// 8. If MFEM was compiled with SuiteSparse, use UMFPACK to solve the system.
137	
138	
139	
140	umf_solver.Mult(*b, x);
141	#endif

Visualization

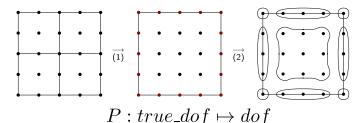
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153	if (visualization)
154	{ · · · · · · · · · · · · · · · · · · ·
155	<pre>char vishost[] = "localhost";</pre>
156	int visport = 19916;
157	<pre>socketstream sol_sock(vishost, visport);</pre>
158	<pre>sol_sock.precision(8);</pre>
159	<pre>sol_sock << "solution\n" << *mesh << x << flush;</pre>
160	}

Example 1 – parallel Laplace equation



Parallel finite element space

122 ParFiniteElementSpace *fespace = new ParFiniteElementSpace(pmesh, fec);



Parallel initial guess, linear/bilinear forms

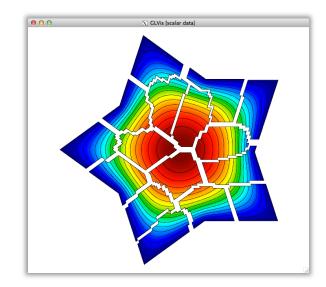
```
130 ParLinearForm *b = new ParLinearForm(fespace);
138 ParGridFunction x(fespace);
147 ParBilinearForm *a = new ParBilinearForm(fespace);
```

Parallel assembly

- Parallel linear solve with AMG
 - 164 // 11. Define and apply a parallel PCG solver for AX=B with the BoomerAMG
 - 165 // preconditioner from hypre.
 - 166 HypreSolver *amg = new HypreBoomerAMG(*A); 167 HyprePCG *pcg = new HyprePCG(*A);
 - 167 HyprePCG *pcg = new HyprePCG(168 pcg->SetTol(le-12);
 - 169 pcg->SetMaxIter(200);
 - 170 pcg->SetPrintLevel(2);
 - 171 pcg->SetPreconditioner(*amg);
 - 172 pcg->Mult(*B, *X);

Visualization

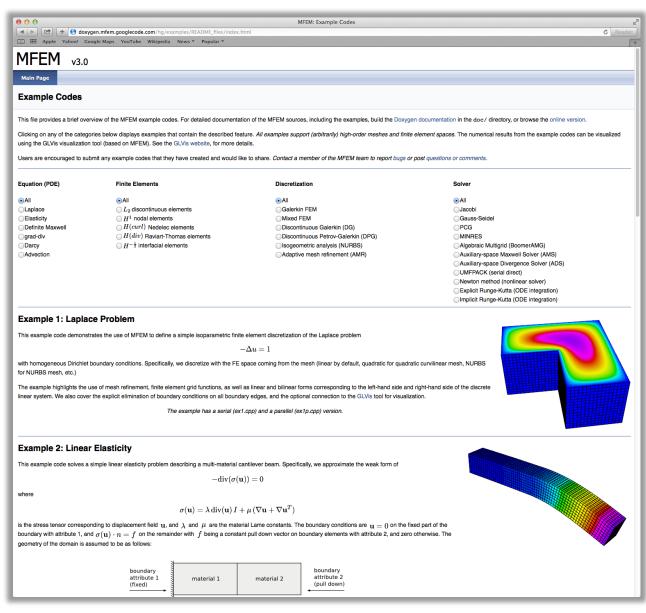
194 // 14. Send the solution by socket to a GLVis server. 195 if (visualization) 196 { 197 char vishost[] = "localhost"; 198 int visport = 19916; 199 socketstream sol_sock(vishost, visport); 200 sol_sock < "parallel " < num_procs < " " << myid << "\n"; 201 sol_sock.precision(8); 202 sol_sock << "solution\n" << *pmesh << x << flush; 203 }



- highly scalable with minimal changes
- build depends on hypre and METIS

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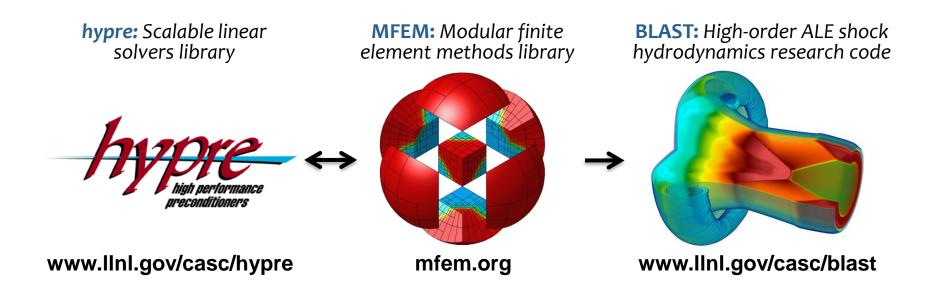
MFEM example codes – mfem.org/examples



Discretization Demo & Lesson

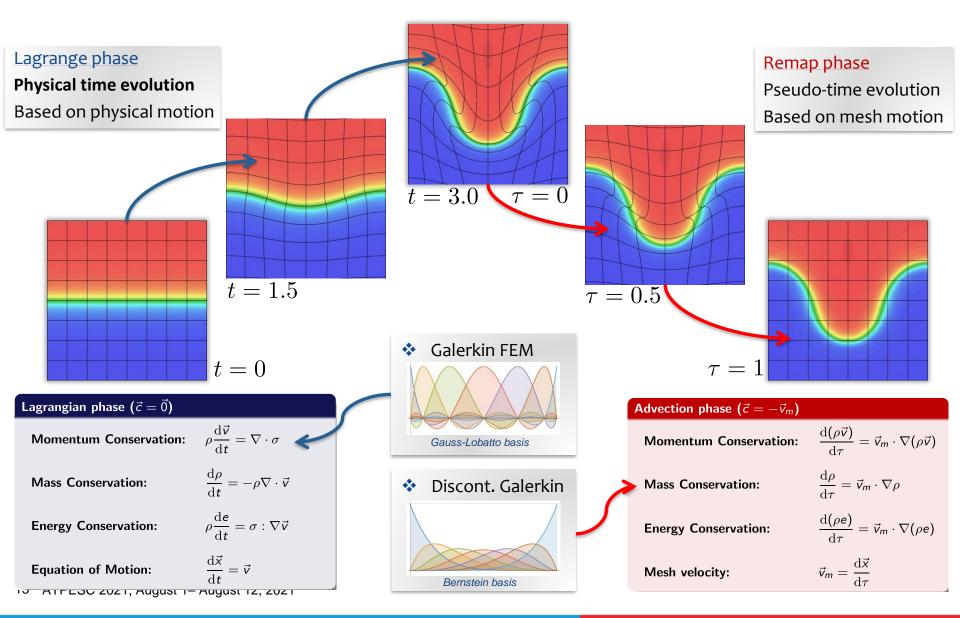
https://xsdk-project.github.io/MathPackagesTraining2021/lessons/mfem_convergence/

Application to high-order ALE shock hydrodynamics

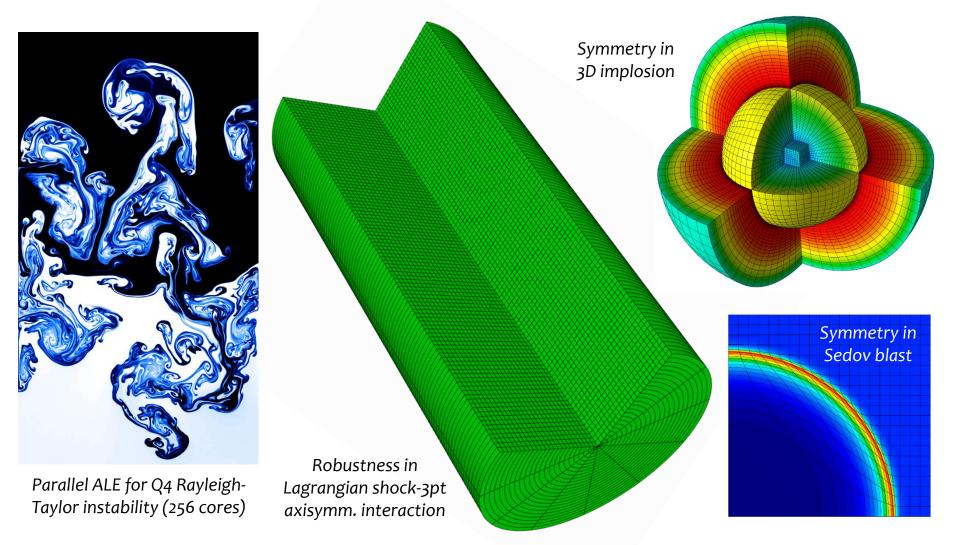


- hypre provides scalable algebraic multigrid solvers
- MFEM provides finite element discretization abstractions
 - uses *hypre's* parallel data structures, provides finite element info to solvers
- BLAST solves the Euler equations using a high-order ALE framework
 - combines and extends MFEM's objects

BLAST models shock hydrodynamics using high-order FEM in both Lagrangian and Remap phases of ALE



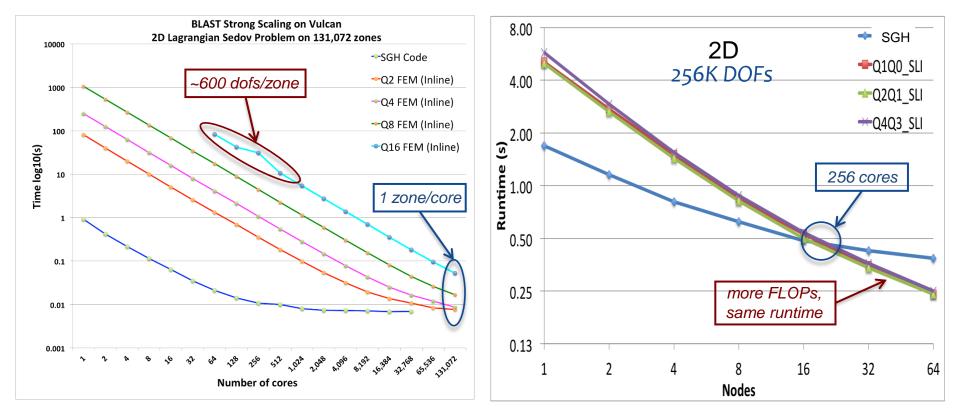
High-order finite elements lead to more accurate, robust and reliable hydrodynamic simulations



High-order finite elements have excellent strong scalability

Strong scaling, p-refinement

Strong scaling, fixed #dofs

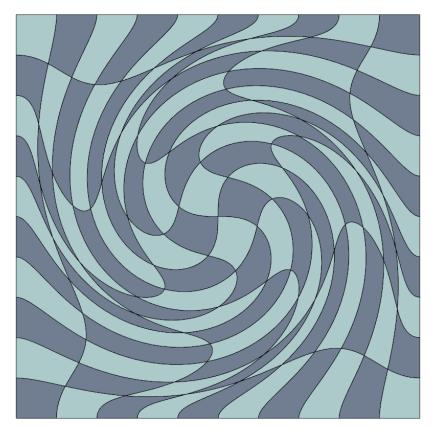


Finite element partial assembly

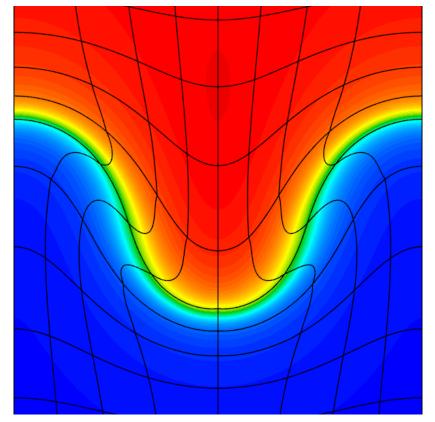
FLOPs increase faster than runtime

Unstructured Mesh R&D: Mesh optimization and highquality interpolation between meshes

We target high-order curved elements + unstructured meshes + moving meshes



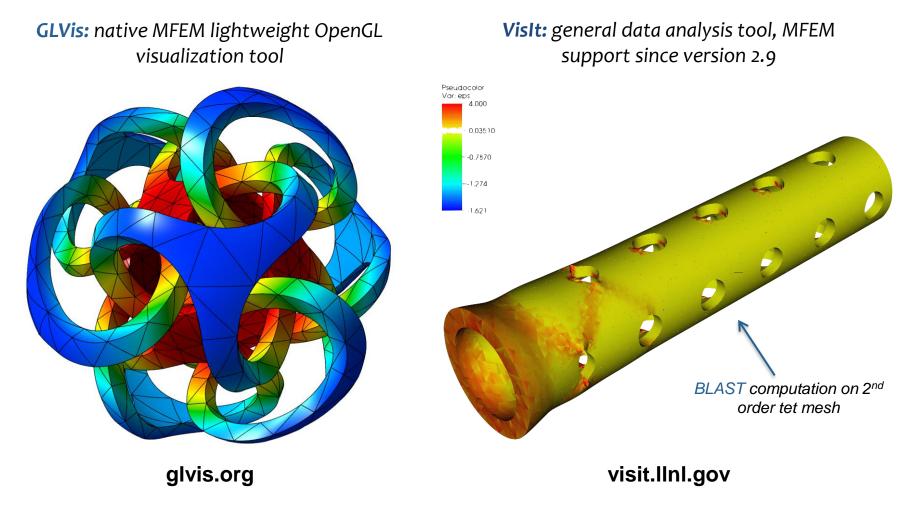
High-order mesh relaxation by neo-Hookean evolution (Example 10, ALE remesh)



DG advection-based interpolation (ALE remap, Example 9, radiation transport)

Unstructured Mesh R&D: Accurate and flexible finite element visualization

Two visualization options for high-order functions on high-order meshes



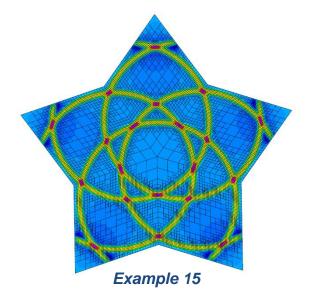
MFEM's unstructured AMR infrastructure

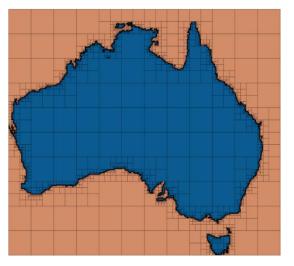
Adaptive mesh refinement on library level:

- Conforming local refinement on simplex meshes
- Non-conforming refinement for quad/hex meshes
- h-refinement with fixed p

General approach:

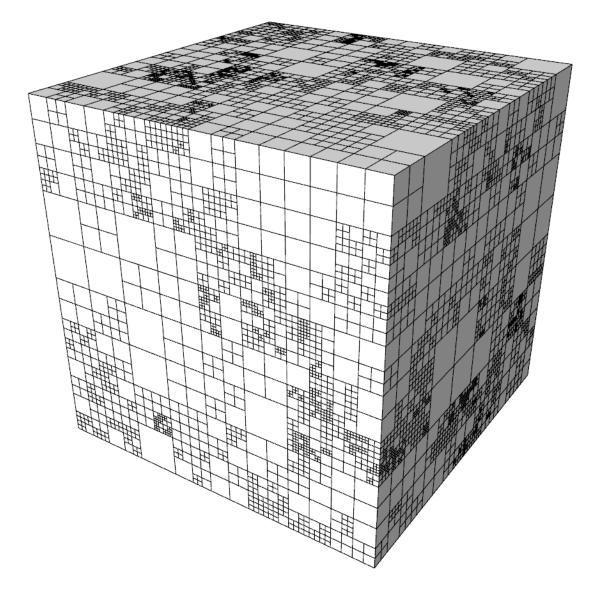
- any high-order finite element space, H1, H(curl),
 H(div), ..., on any high-order curved mesh
- 2D and 3D
- arbitrary order hanging nodes
- anisotropic refinement
- derefinement
- serial and parallel, including parallel load balancing
- independent of the physics (easy to incorporate in applications)



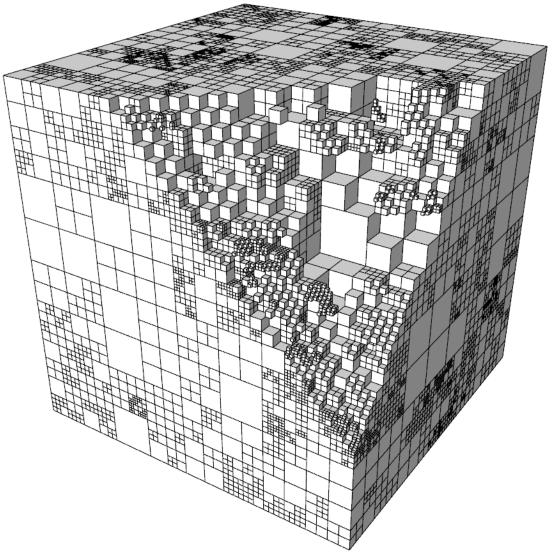


Shaper miniapp

Nonconforming variational restriction

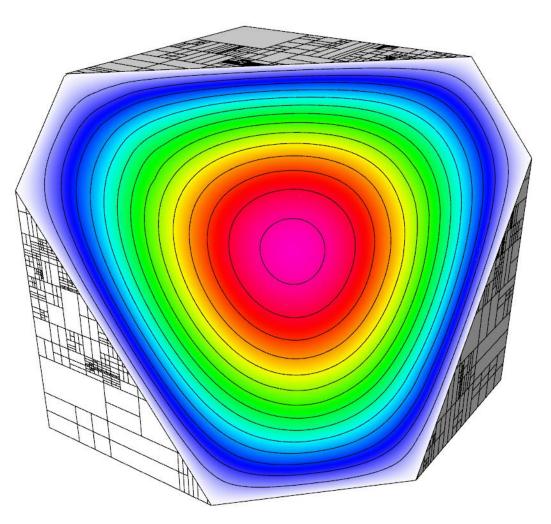


Nonconforming variational restriction



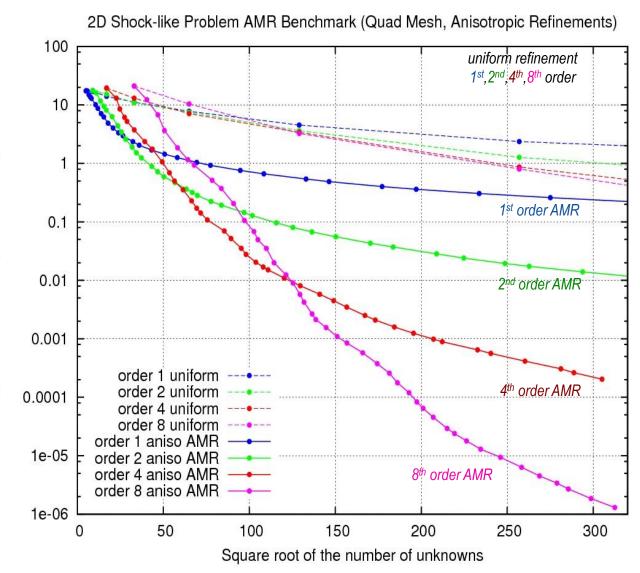
Regular assembly of A on the elements of the (cut) mesh

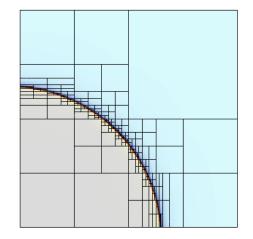
Nonconforming variational restriction

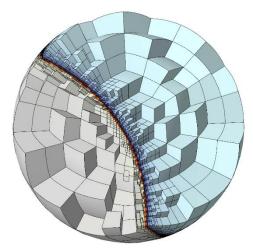


Conforming solution y = P x

AMR = smaller error for same number of unknowns

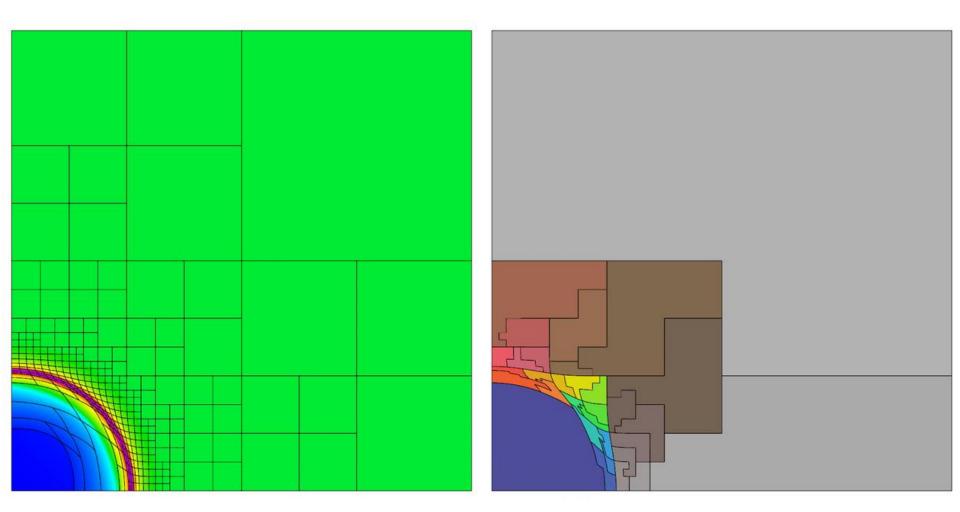






Anisotropic adaptation to shock-like fields in 2D & 3D

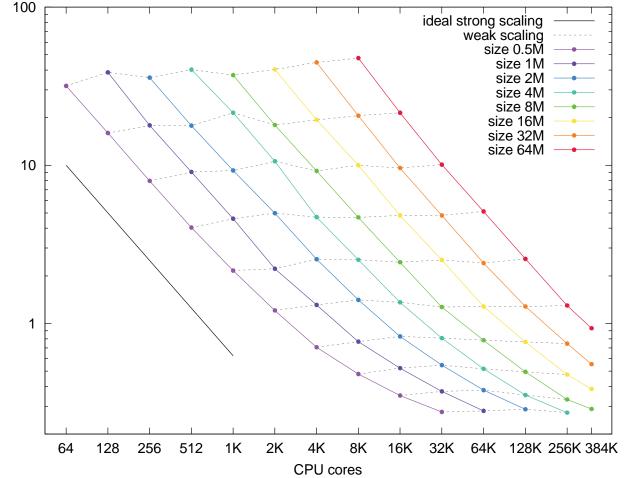
Parallel dynamic AMR, Lagrangian Sedov problem

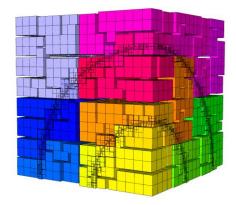


Adaptive, viscosity-based refinement and derefinement. 2nd order Lagrangian Sedov

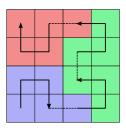
Parallel load balancing based on spacefilling curve partitioning, 16 cores

Parallel AMR scaling to ~400K MPI tasks





Parallel decomposition (2048 domains shown)

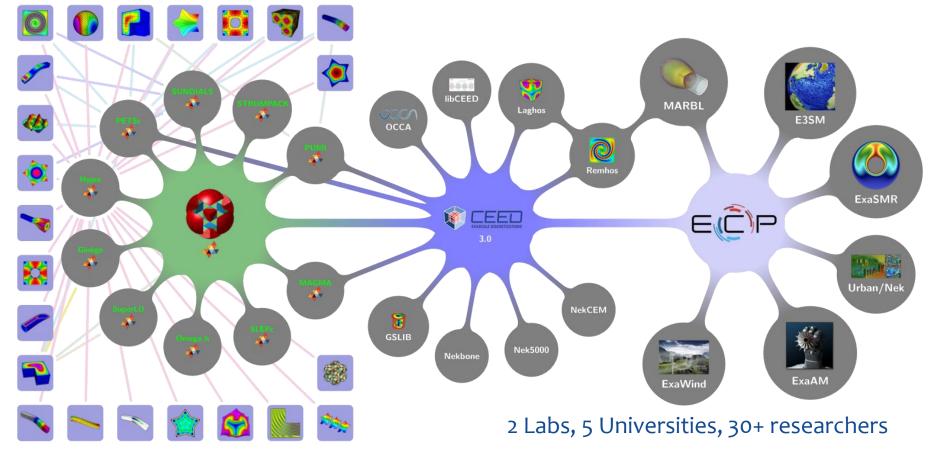


Parallel partitioning via Hilbert curve

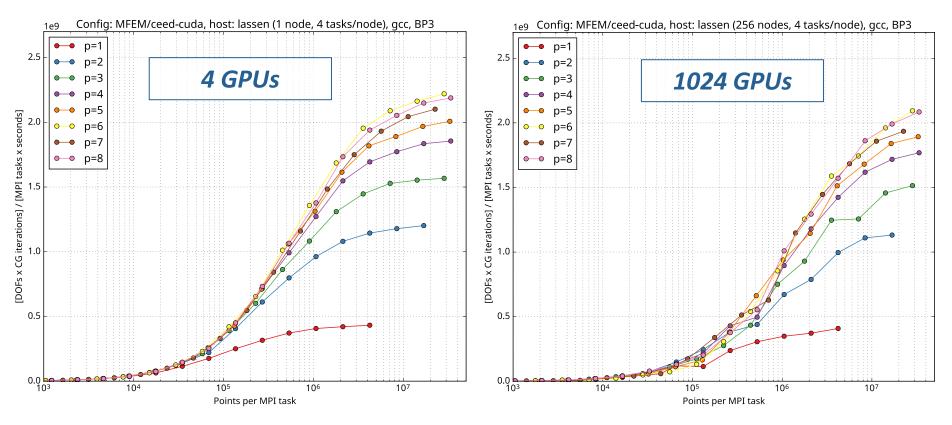
- weak+strong scaling up to ~400K MPI tasks on BG/Q
- measure AMR only components: interpolation matrix, assembly, marking, refinement & rebalancing (no linear solves, no "physics")

EXASCALE DISCRETIZATIONS

ceed.exascaleproject.org



MFEM Scaling on Multiple GPUs



Largest problem size: 34 billion; Best total performance: 2.1 TDOF/s

MFEM-BP3, 3D, Lassen 4 x V100 GPUs / node

Resources

More information and publications

- MFEM mfem.org
- MFEM Project github.com/mfem
- MFEM Repo github.com/mfem/mfem
- MFEM Issues github.com/mfem/mfem/issues
- BLAST computation.llnl.gov/projects/blast
- CEED ceed.exascaleproject.org
- Virtual Community Workshop (Oct 20, 2021)
 - Website mfem.org/workshop
 - Technical presentations from MFEM team
 - Contributed talks from application devs
 - Demos of MFEM through python, and Jupyter notebooks
 - Discussions of development roadmap, and application areas



Q4 Rayleigh-Taylor singlematerial ALE on 256 processors

27 ATPESC 2021, August 1– August 12, 2021

This work performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344. LLNL-PRES-755924

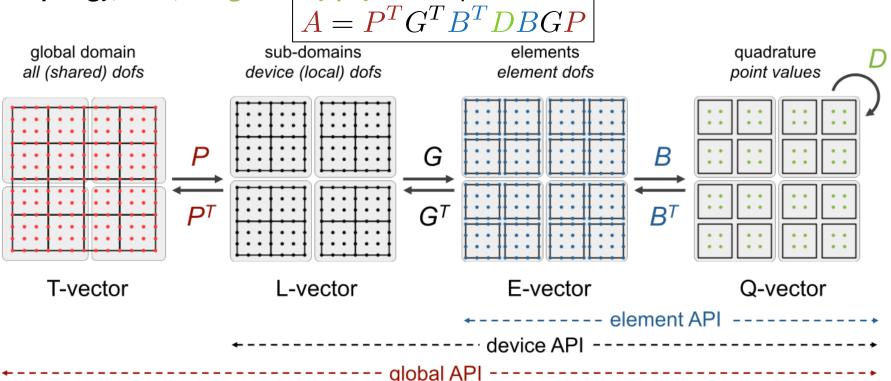
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Fundamental finite element operator decomposition

The assembly/evaluation of FEM operators can be decomposed into **parallel**, **mesh topology**, **basis**, and **geometry/physics** components:

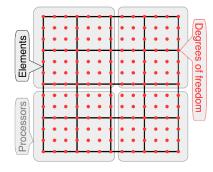


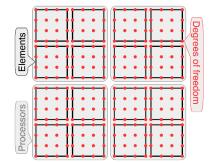
- partial assembly = store only D, evaluate B (tensor-product structure)
- better representation than A: optimal memory, near-optimal FLOPs
- purely algebraic, applicable to many apps

CEED high-order benchmarks (BPs)

- CEED's bake-off problems (BPs) are high-order kernels/benchmarks designed to test and compare the performance of high-order codes.
 BP1: Solve {Mu=f}, where {M} is the mass matrix, q=p+2
 BP2: Solve the vector system {Mu_i=f_i} with {M} from BP1, q=p+2
 BP3: Solve {Au=f}, where {A} is the Poisson operator, q=p+2
 BP4: Solve the vector system {Au_i=f_i} with {A} from BP3, q=p+2
 BP5: Solve {Au=f}, where {A} is the Poisson operator, q=p+1
 BP6: Solve the vector system {Au_i=f_i} with {A} from BP3, q=p+1
- Compared Nek and MFEM implementations on BG/Q, KNLs, GPUs.
- Community involvement deal.ii, interested in seeing your results.
- Goal is to learn from each other, benefit all CEED-enabled apps.

github.com/ceed/benchmarks





BP terminology: T- and Evectors of HO dofs

Tensorized partial assembly

$$B_{ki} = \varphi_i(q_k) = \varphi_{i_1}^{1d}(q_{k_1})\varphi_{i_2}^{1d}(q_{k_2}) = B_{k_1i_1}^{1d}B_{k_2i_2}^{1d}$$

$$U_{k_1k_2} = B_{k_1i_1}^{1d} B_{k_2i_2}^{1d} V_{i_1i_2} \mapsto U = B^{1d} V (B^{1d})^T$$

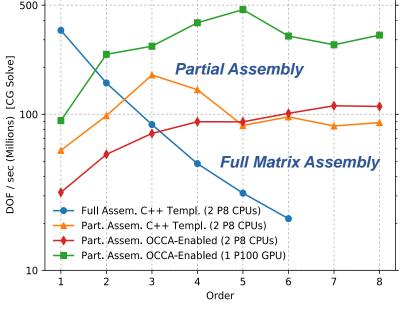
p- order,	d – mesh dim,	$O(p^d) - dofs$
-----------	---------------	-----------------

Method	Memor y	Assemb ly	Action
Full Matrix Assembly	$O(p^{2d})$	$O(p^{3d})$	$O(p^{2d})$
Partial Assembly	$O(p^d)$	$O(p^d)$	$O(p^{d+1})$

Storage and floating point operation scaling for different assembly types

Poisson CG solve performance with different assembly types (higher is better)

Full matrix performance drops sharply at high orders while partial assembly scales well!



This work performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344. LLNL-PRES-755924

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FASTMath Unstructured Mesh Technologies

K.D. Devine¹, V. Dobrev², D.A. Ibanez¹, T. Kolev², K.E. Jansen³,

O. Sahni⁴, M.S. Shephard⁴, G.M. Slota⁴, C.W. Smith⁴

¹Sandia National Laboratories

²Lawrence Livermore National Laboratory

³University of Colorado

⁴Rensselaer Polytechnic Institute





ATPESC Numerical Software Track













Unstructured Mesh Methods

Unstructured mesh – a spatial domain discretization composed of topological entities with general connectivity and shape

Advantages

- Automatic mesh generation for any level of geometric complexity
- Can provide the highest accuracy on a per degree of freedom basis
- General mesh anisotropy possible
- Meshes can easily be adaptively modified
- Given a complete geometry, with analysis attributes defined on that model, the entire simulation work flow can be automated

Disadvantages

- More complex data structures and increased program complexity, particularly in parallel
- Requires careful mesh quality control (level depend required a function of the unstructured mesh analysis code)
- Poorly shaped elements increase condition number of global system – makes matrix solves harder
- Non-tensor product elements not as computationally efficient

Unstructured Mesh Methods

Goal of FASTMath unstructured mesh developments include:

- Provide unstructured mesh components that are easily used by application code developers to extend their simulation capabilities
- Ensure those components execute on exascale computing systems and support performant exascale application codes
- Develop components to operate through multi-level APIs that increase interoperability and ease of integration
- Address technical gaps by developing tools that address needs and/or eliminate/minimize disadvantages of unstructured meshes
- Work with DOE application developers on integration of these components into their codes

FASTMath Unstructured Mesh Developments

Technology development areas:

- Unstructured Mesh Analysis Codes Support application's PDE solution needs – MFEM library is a key example
- Performant Mesh Adaptation Parallel mesh adaptation to integrate into analysis codes to ensure solution accuracy
- Dynamic Load Balancing and Task Management Technologies to ensure load balance and effectively execute by optimal task placement
- Unstructured Mesh for PIC Tools to support PIC on unstructured meshes
- Unstructured Mesh ML and UQ ML for data reduction, adaptive mesh UQ
- In Situ Vis and Data Analytics Tools to gain insight as simulations execute
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FASTMath Unstructured Mesh Tools and Components

- FE Analysis codes
 - MFEM (https://mfem.org/)
 - LGR (https://github.com/SNLComputation/lgrtk)
 - PHASTA (https://github.com/phasta/phasta)
- Unstructured Mesh Infrastructure
 - Omega_h (<u>https://github.com/SNLComputation/omega_h</u>)
 - PUMI/MeshAdapt (https://github.com/SCOREC/core)
 - PUMIpic (<u>https://github.com/SCOREC/pumi-pic</u>)
- Load balancing, task placement
 - Zoltan (<u>https://github.com/sandialabs/Zoltan</u>)
 - Zoltan2 (<u>https://github.com/trilinos/Trilinos/tree/master/packages/zoltan2</u>)
 - Xtra-PULP (<u>https://github.com/HPCGraphAnalysis/PuLP</u>)
 - EnGPar (<u>http://scorec.github.io/EnGPar/</u>)
- Unstructured Mesh PIC applications
 - XGCm (<u>https://github.com/SCOREC/xgcm</u>) private repo
 - GITRm (<u>https://github.com/SCOREC/gitrm</u>) private repo
- 37 ATPESC 2021, August 1- August 12, 2021

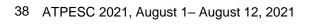
Parallel Unstructured Mesh Infrastructure

Support unstructured mesh interactions on exascale systems

- Mesh hierarchy to support interrogation and modification
- Maintians linkage to original geometry
- Conforming mesh adaptation
- Inter-process communication
- Supports field operations

Tools

- Omega_h full CPU/GPU support
- PUMI CPU based curved mesh adapt.
- PUMIPic Unstructured mesh with particles for GPU implementations



Geometric model

Partition model

P1

inter-process part

boundary

Proc i

intra-process part

boundary

P₀

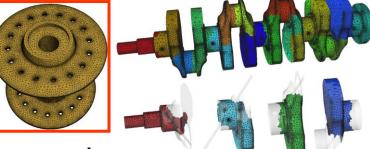
Proc *j*

 P_2

Mesh Generation and Control

Mesh Generation:

- Automatically mesh complex domains should work directly from CAD, image data, etc.
- Use tools like Gmsh, Simmetrix, etc.
 Mesh control:

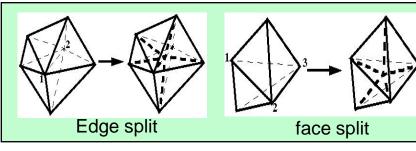


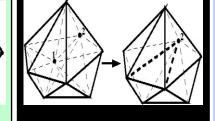
- Use a posteriori information to improve mesh
- Curved geometry and curved mesh entities
- Support full range of mesh modifications vertex motion, mesh entity curving, cavity based refinement and coarsening, etc. anisotropic adaptation
- Control element shapes as needed by the various discretization methods for maintaining accuracy and efficiency

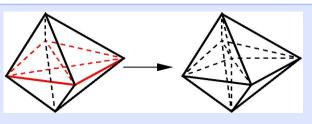
Parallel execution of all functions is critical on large meshes

General Mesh Modification for Mesh Adaptation

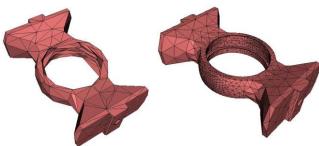
- Driven by an anisotropic mesh size field that can be set by any combination of criteria
- Employ a "complete set" of mesh modification operations to alter the mesh into one that matches the given mesh size field
- Advantages
 - Supports general anisotropic meshes
 - Can obtain level of accuracy desired
 - Can deal with any level of geometric domain complexity
 - Solution transfer can be applied incrementally provides more control to satisfy conservation constraints







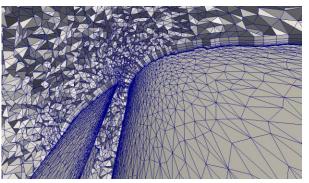
Double split collapse to remove sliver

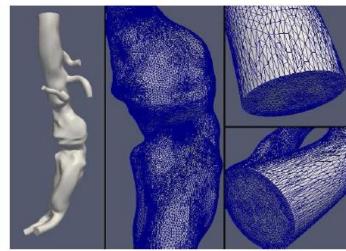


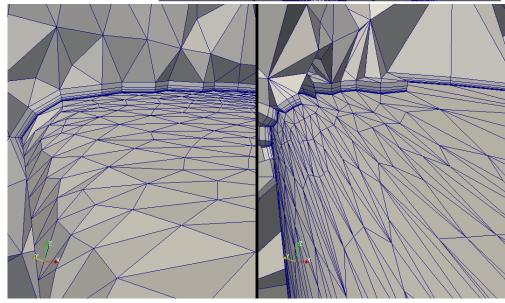
Mesh Adaptation Status

- Applied to very large scale models

 92B elements on 3.1M processes
 on ³/₄ million cores
- Local solution transfer supported through callback
- Effective storage of solution fields on meshes
- Supports adaptation with boundary layer meshes





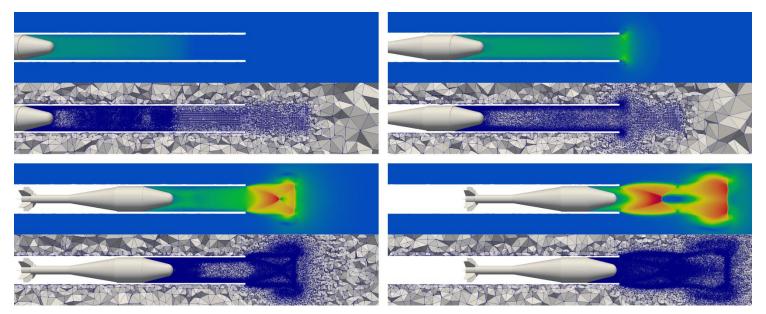


Mesh Adaptation of Evolving Geometry Problems

Many applications have geometry that evolves as a function of the results – Effective adaptive loops combine mesh motion and mesh modification

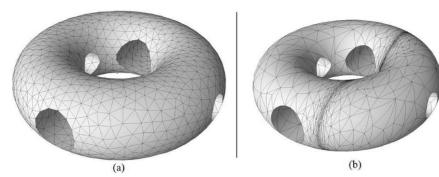
Adaptive loop:

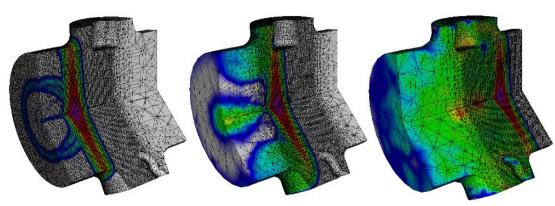
- 1. Initialize analysis case, generate initial mesh, start time stepping loop
- 2. Perform time steps employing mesh motion monitor element quality and discretization errors
- 3. When element quality is not satisfactory or discretization errors too large set mesh size field and perform mesh modification
- 4. Return to step 2.

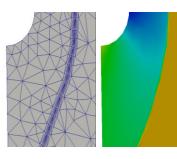


Mesh Adaptation

- Supports adaptation of curved elements
- Adaptation based on multiple criteria, examples
 - Level sets at interfaces
 - Tracking particles
 - Discretization errors
 - Controlling element shape in evolving geometry



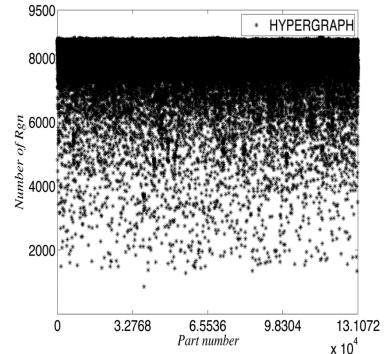






Load Balancing, Dynamic Load balancing

- Purpose: Balance, rebalance computational load while controlling communications
 - Equal "work load" with minimum inter-process communications
- FASTMath load balancing tools
 - Zoltan/Zoltan2 libraries provide multiple dynamic partitioners with general control of partition objects and weights
 - EnGPar diffusive multi-criteria partition improvement
 - XtraPuLP multi-constraint
 Part number
 x 10⁴
 multi-objective label propagation-based graph partitioner



Architecture-aware partitioning and task mapping

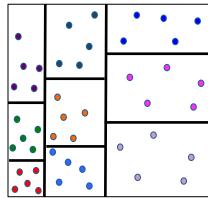
Reduce application communication time at extreme scale

- *Partitioning and load balancing*: assign work to processes in ways that avoid process idle time and minimize communication
- Task mapping: assign processes to cores in ways that reduce messages distances and network congestion
- Important in extreme-scale systems:
 - Small load imbalances can waste many resources
 - Large-scale networks can cause messages to travel long routes and induce congestion
- *Challenge* to develop algorithms that...
 - account for underlying architectures & hierarchies
 - run effectively side-by-side with application across many platforms (multicore, GPU)

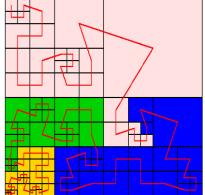
Zoltan/Zoltan2 Toolkits: Partitioners

Suite of partitioners supports a wide range of applications; no single partitioner is best for all applications.

Geometric

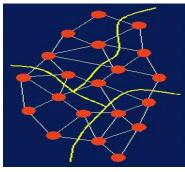


Recursive Coordinate Bisection Recursive Inertial Bisection Multi-Jagged Multi-section



Space Filling Curves

Topology-based



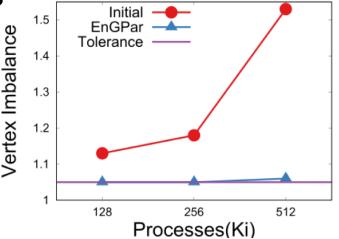
PHG Graph Partitioning Interface to ParMETIS (U. Minnesota) Interface to PT-Scotch (U. Bordeaux)

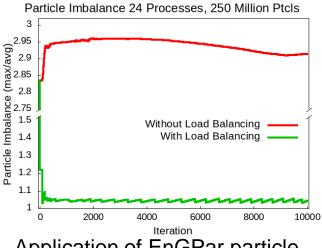
> PHG Hypergraph Partitioning Interface to PaToH (Ohio St.)

EnGPar Dynamic Load Balancing

Quickly reduces large imbalances on (hyper)graphs with billions of edges on up to 512K processes

- Multi-(hyper)graph supports multiple dependencies (edges) between application work/data items (vertices)
- Application defined vertex and edges
- Diffusion sends from heavily loaded parts to lighter parts
- On a 1.3B element mesh, in 8 seconds EnGPar reduces a 53% vtx imbalance to 6%, elm imbalance of 5%, edge cut increase by 1%
- Applied to PIC calculations to support particle balance – flexibility of vertex and edge definition critical to attaining 20% reduction in total run time





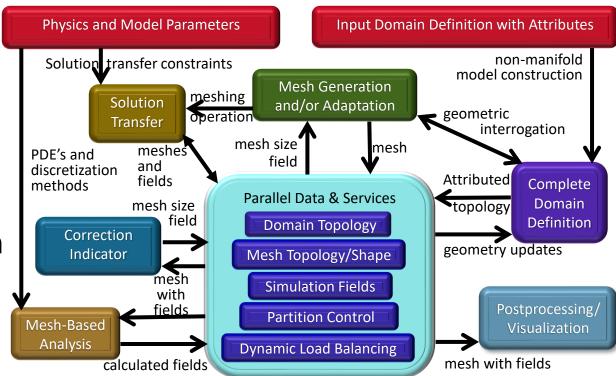
Application of EnGPar particle dynamic load balancing in a GITRm impurity transport simulation

Creation of Parallel Adaptive Loops

Parallel data and services are the core

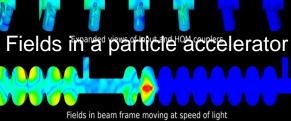
- Geometric model topology for domain linkage
- Mesh topology it must be distributed
- Simulation fields distributed over geometric model and mesh
- Partition control
- Dynamic load balancing required at multiple steps
- API's to link to
 - CAD
 - Mesh generation and adaptation
 - Error estimation

– etc



Parallel Adaptive Simulation Workflows

- Automation and adaptive methods critical to reliable simulations
- In-memory examples
 - MFEM High order
 FE framework
 - PHASTA FE for NS
 - FUN3D FV CFD
 - Proteus multiphase FE
 - Albany FE framework
 - ACE3P High order FE electromagnetics
 - M3D-C1 FE based MHD
 - Nektar++ High order FE flow

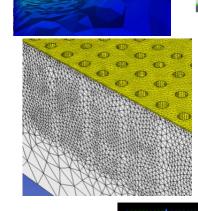


ILC cryomodule of 8 Superconducting RF cavities



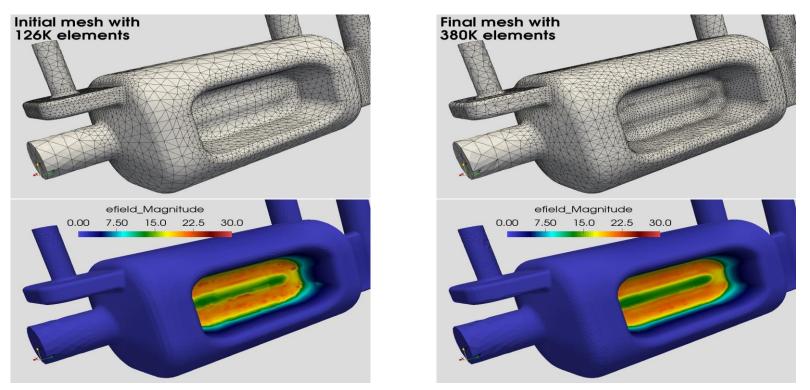
Blood flow on the

arterial system



Application interactions – Accelerator EM

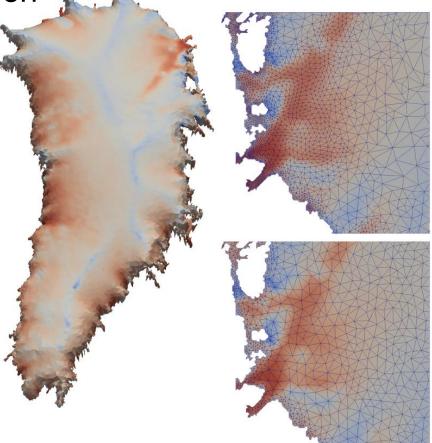
Omega3P Electro Magnetic Solver (second-order curved meshes)



This figure shows the adaptation results for the CAV17 model. (top left) shows the initial mesh with ~126K elements, (top right) shows the final (after 3 adaptation levels) mesh with ~380K elements, (bottom left) shows the first eigenmode for the electric field on the initial mesh, and (bottom right) shows the first eigenmode of the electric field on the final (adapted) mesh.

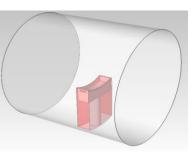
Application interactions – Land Ice

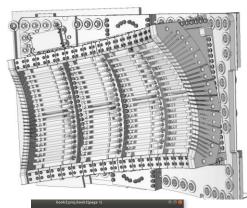
- FELIX, a component of the Albany framework is the analysis code
- Omega_h parallel mesh adaptation is integrated with Albany to do:
 - Estimate error
 - Adapt the mesh
- Ice sheet mesh is modified to minimize degrees of freedom
- Field of interest is the ice sheet velocity



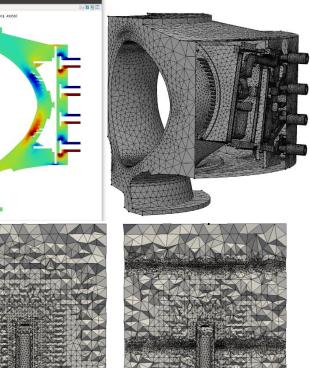
Application interactions – RF Fusion

- Accurate RF simulations require
 - Detailed antenna CAD geometry
 - CAD geometry defeaturing
 - Extracted physics curves from EFIT
 - Faceted surface from coupled mesh
 - Analysis geometry combining CAD, physics geometry and faceted surface
 - 3D meshes for accurate FE calculations in MFEM
 - Projection based error estimator
 - Conforming mesh adaptation with PUMI





CAD model of antenna array



52 ATPESC 2021, August 1- August 12, 2021

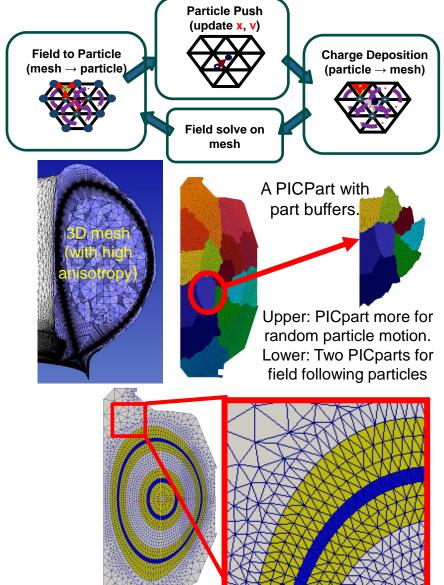
Initial Mesh

Final Adapted

Supporting Unstructured Mesh for Particle-in-Cell Calculations

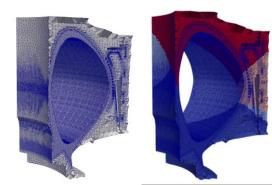
PUMIPic data structures are mesh centric

- Mesh is distributed as needed by the application in terms of PICparts
- Mesh can be graded and anisotropic
- Particle data associated with elements
- Operations take advantage of distributed mesh topology
- Mesh distributed in PICparts
 - Start with a partition of mesh into a set of "core parts"
 - A PICpart is defined by a "core part" and sufficient buffer to keep particles on process for one or more pushes
 - GPU version defines buffer as set of neighboring parts – dramatic reduction in memory and communication costs

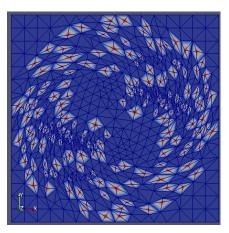


Mesh Data Structure for Heterogeneous Systems

- Mesh topology/adaptation tool Omega
 - Conforming mesh adaptation (coarsening past initial mesh, refinement, swap)
 - Manycore and GPU parallelism using Kokkos, CUDA, or HIP
 - Distributed mesh via mesh partitions with MPI communications
 - Support for mesh-based fields
- Recent RPI developments:
 - Mixed mesh adjacency storage and query
 - Two-way mesh matching for periodic BC
 - Ported and tested on AMD GPUs using HIP



Serial and RIB partitioned mesh of RF antenna and vessel model.



Adaptation following rotating flow field.

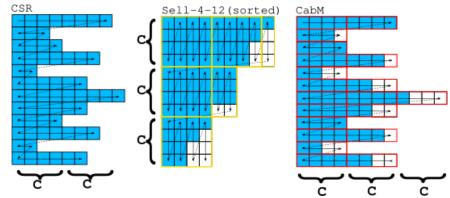
triangle	0			1		
adj vertex	0	1	3	2	3	1

adj triangle 0 0 1 1 0 1offset 0 1 3 4 6vertex 0 1 2 3

Mesh entity adjacency arrays.

PUMIPic Particle Data Structures

- Layout of particles in memory is critical to performance. Requirements:
 - Optimizes push (sort/rebuild), scatter, and gather operations
 - Associates particles with mesh elements
 - Changes in the number of particles per element
 - Evenly distributes work with a range of particle distributions (e.g. uniform, Gaussian, exponential, etc.)
 - Stores a lot of particles per GPU low overhead
- Particle data structure interface and implementation
 - API abstracts implementation for PIC code developers
 - CSR, Sell-C-σ, CabanaM
 - Performance is a function of particle distribution
 - Cabana AoSoA w/a CSR index of elements-to-particles are promising

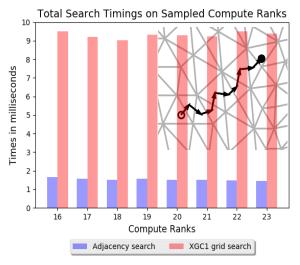


Left to Right: CSR, SCS with vertical slicing (yellow boxes), CabanaM (red boxes are SOAs). C is a team of threads.

PIC Operations Supported by PUMIPic

- Particle push
- Adjacency based search
 - Faster than grid based search
- Element-to-particle association update
- Particle Migration
- Particle path visualization
- Mesh partitioning w/buffer regions
- Mesh field association
- Poisson field solve using PETSc DMPlex on GPUs
- Checkpoint/restart of particle and mesh data supports customization for each application

2020 PUMIPic Paper: https://www.scorec.rpi.edu/REPORTS/2020-2.pdf

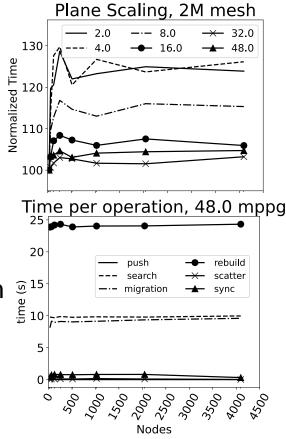


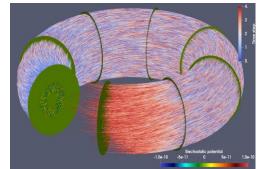
PUMIPic based XGCm Edge Plasma Code

XGCm is a version of XGC being built on PUMIPic

- 2M elements, 1M vertices, 2 to 128 poloidal planes Pseudo push and particle-to-mesh avro activity Tested on up to 24 ^{crea} Testing of PUMIPic for use in XGC like push

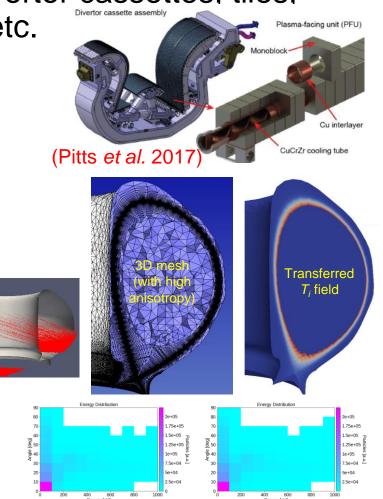
- trillion particles, for 100 iterations: push, adjacency
- Weak scaling up to 24576 GPUs (4096 nodes) with 48 million particles per GPU
- XGCm status: All operations on GPU
- Ion and electron charge scatter and push
- Electrostatic potential calculation
- Gyro-kinetic electric field calculation and gather
- Poisson solve





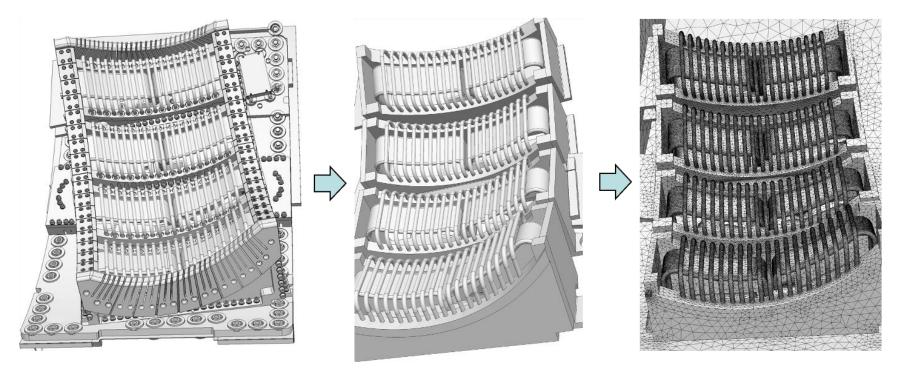
PUMIPic based GITRm Impurity Transport Code

- Incorporates impurity transport capabilities of GITR
- 3D mesh for cases such including divertor cassettes, tiles, limiters, specific diagnostics/probes etc.
- Status
 - Physics equivalent to GITR
 - Particle initialization directly on 3D mesh
 - 3D mesh design/control including anisotropy to properly represent the background fields
 - Field transfer from SOLPS to 3D mesh
 - Non-uniform particle distribution
 evolves quickly in time
 - Load balancing particles via EnGPar
 - Distance to boundary for sheath E field
 - Post-processing on 3D unstructured mesh



Hands-on Exercise: Workflow Introduction

Exercising Simmetrix and PUMI tools for model preparation and mesh generation on a complex CAD model



https://xsdk-project.github.io/ATPESC2021HandsOnLessons/lessons/pumi/